

BA'ZI AMALIY MASALALAR DIFFERENSIAL  
TENGLAMALARINI MATHCAD DASTURI YORDAMIDA  
SONLI YECHISH

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**Annotatsiya:** ushbu tezisda amaliy ahamiyatga ega bo'lgan differensial tenglamalarni sonli yechishda mathcad dasturidan foydalanish yo'llari ko'rsatilgan bo'lib, bunga doir bir nechta misollar sonli yechib ko'rsatilgan.

**Annotation:** In this thesis, the ways of loading from the mathcad program in the numerical solution of differential equations, which have a practice, are indicators, and several examples of this are numerical solutions.

**Аннотация:** В данной диссертации способы загрузки из программы mathcad при численном решении дифференциальных уравнений, имеющие практику, являются индикаторами, и несколько примеров тому являются численными решениями.

*Kalit so'zlar:* Differensial, hosila, rkfixed, integral, rkadapt, mathcad.

*Key words:* Differential, derivative, rkfixed, integral, rkadapt, mathcad.

*Ключевые слова:* Дифференциал, производная, rkfixed, интеграл, rkadapt, mathcad.

Birinchi tartibli hosilaga nisbatan yechilgan oddiy differensial tenglamalar yoki tenglamalar sistemasini yechish uchun o'zgarmas qadamli to'rtinchi tartibli Runge-Kutta usulini ifodalovchi *rkfixed* funksiyadan foydalaniladi, bu funksiya yozilishining umumiy ko'rinishi quyidagicha:

$\text{rkfixed}(y, x_1, x_2, \text{npoints}, D)$

bu yerda  $y$  – boshlang'ich shartlar vektori;  $[x_1, x_2]$  – integrallash intervali; npoints

– hisoblanadigan nuqtalar soni (boshlang'ich nuqta bunga kirmaydi);  $D$  – vektor (tenglamalar sistemasi o'ng tomonining vektor-funksiyasi).

**1- misol.** Mexanik sistema tebranishini ifodalovchi ushbu

$$\frac{dy}{dx} = \sin x + \frac{1}{y}$$

oddiy differensial tenglamani  $y(0)=1$  boshlang'ich shart uchun  $[0;6]$  intervalda Mathcad paketi yordamida yeching.

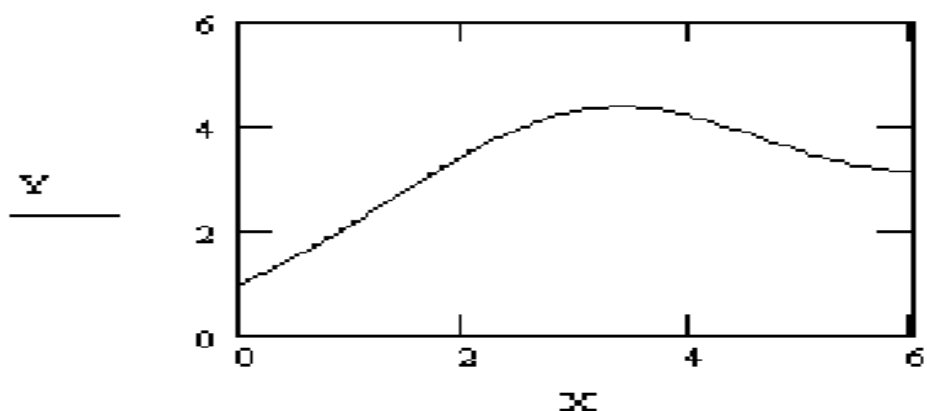
**Yechish.**

$$y_0 := 1$$

$$D(x, y) := \sin(x) + \frac{1}{y_0}$$

$$Z := \text{rkfixed}(y_0, 0, 6, 100, D)$$

$$X := Z \{0\} \quad Y := Z \{1\}$$



**2-misol.** Mexanik sistema tebranishini ifodalovchi ushbu

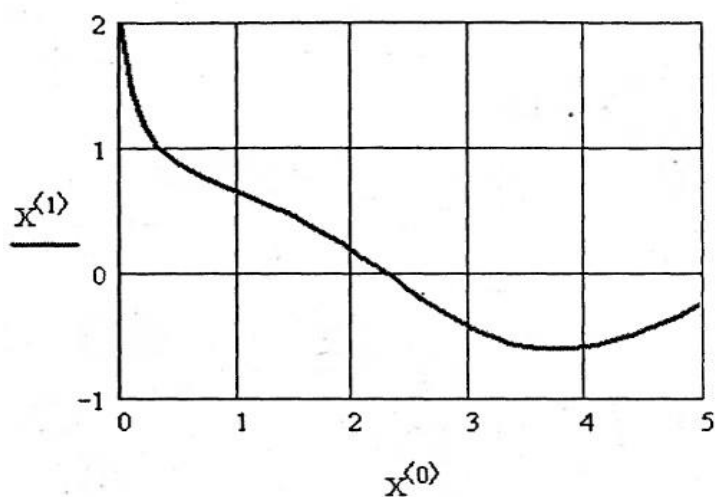
$$x' + x + x^3 = \cos(t)$$

oddiy differensial tenglamani  $x(0)=2$  boshlang'ich shart Mathcad paketi yordamida yeching.

**Yechish.**

$$D(t, x) := -x - x^3 + \cos(t)$$

$$X := \text{rkfixed}(2, 0, 5, 50, D)$$



1) Birinchi tartibli hosilaga nisbatan yechilgan oddiy differensial tenglamalar yoki tenglamalar sistemasini yechish uchun avtomatik tanlanuvchan qadamli to'rtinchi tartibli Runge-Kutta usulini ifodalovchi *rkadapt* funksiyadan foydalaniladi, bu funksiya yozilishining umumiy ko'rinishi quyidagicha:

$$\text{rkadapt}(y, x_1, x_2, \text{eps}, D, \text{kmax}, \text{nt})$$

bu yerda  $y$  – boshlang'ich shartlar vektori;  $[x_1, x_2]$  – integrallash intervali;  $\text{eps}$  – hisoblash aniqligi;  $D$  – vektor (tenglamalar sistemasi o'ng tomonining vektor-funksiyasi);  $\text{kmax}$  – natija matritsasidagi satrlar soni (bitta nuqtada hisoblash uchun  $\text{kmax}=2$ );  $\text{nt}$  – integrallash qadamining minimal qiymati.

2) Birinchi tartibli hosilaga nisbatan yechilgan oddiy differensial tenglamalar yoki tenglamalar sistemasini yechish uchun to'rtinchi tartibli Runge-Kutta usulini ifodalovchi *Rkadapt* funksiyadan foydalaniladi, bu funksiya yozilishining umumiy ko'rinishi quyidagicha:

$$\text{Rkadapt}(y, x_1, x_2, \text{npoints}, D)$$

Bu yerda  $y$  – boshlang'ich shartlar vektori;  $[x_1, x_2]$  – integrallash intervali;  $\text{npoints}$  – hisoblanadigan nuqtalar soni (boshlang'ich nuqta bunga kirmaydi);  $D$  – vektor (tenglamalar sistemasi o'ng tomonining vektor-funksiyasi).

**3-misol.** Mexanik sistema tebranishini ifodalovchi ushbu

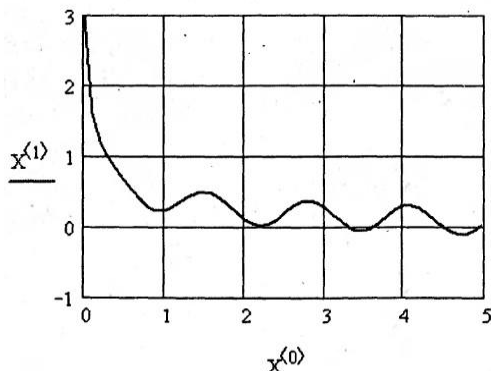
$$x' = -x^3 - x^2 + \cos(5t)$$

oddiy differensial tenglamani  $x(0)=3$  boshlang'ich shart Mathcad paketi yordamida yeching.

**Yechish.**

$$D(t, x) := -x^3 - x^2 + \cos(5t)$$

$$X := \text{Rkadapt}(3, 0, 5, 50, D)$$



|    | 0   | 1     |
|----|-----|-------|
| 0  | 0   | 3     |
| 1  | 0.1 | 1.612 |
| 2  | 0.2 | 1.217 |
| 3  | 0.3 | 0.993 |
| 4  | 0.4 | 0.819 |
| 5  | 0.5 | 0.661 |
| 6  | 0.6 | 0.515 |
| 7  | 0.7 | 0.387 |
| 8  | 0.8 | 0.29  |
| 9  | 0.9 | 0.238 |
| 10 | 1   | 0.235 |
| 11 | 1.1 | 0.277 |
| 12 | 1.2 | 0.35  |
| 13 | 1.3 | 0.427 |
| 14 | 1.4 | 0.485 |
| 15 | 1.5 | 0.504 |

Ko'plab amaliy masalalar differensial tenglamasini analitik yechishda birmuncha murakkabliklarga duch kelinadi, shunday xolatlarda mathcad dasturi yordamida differensial tenglamalarning sonli yechimini toppish mumkin ekan.

#### **FOYDALANILGAN ADABIYOTLAR RO'YXATI**

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